

The density of a fluid is defined as its mass per unit volume.

### 1.4.1 Density

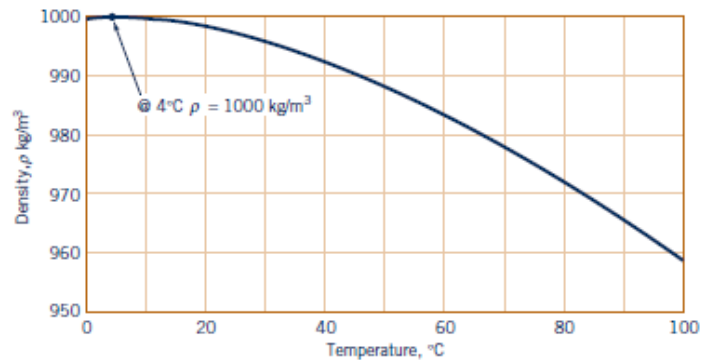
The *density* of a fluid, designated by the Greek symbol  $\rho$  (rho), is defined as its mass per unit volume. Density is typically used to characterize the mass of a fluid system. In the BG system,  $\rho$  has units of slugs/ft<sup>3</sup> and in SI the units are kg/m<sup>3</sup>.

The value of density can vary widely between different fluids, but for liquids, variations in pressure and temperature generally have only a small effect on the value of  $\rho$ . The small change in the density of water with large variations in temperature is illustrated in Fig. 1.3. Tables 1.5 and 1.6 list values of density for several common liquids. The density of water at 60 °F is 1.94 slugs/ft<sup>3</sup> or 999 kg/m<sup>3</sup>. The large difference between those two values illustrates the importance of paying attention to units! Unlike liquids, the density of a gas is strongly influenced by both pressure and temperature, and this difference will be discussed in the next section.

The *specific volume*,  $v$ , is the *volume* per unit mass and is therefore the reciprocal of the density—that is,

$$v = \frac{1}{\rho} \quad (1.5)$$

This property is not commonly used in fluid mechanics but is used in thermodynamics.



■ **Figure 1.3** Density of water as a function of temperature.

## 1.4.2 Specific Weight

Specific weight is weight per unit volume; specific gravity is the ratio of fluid density to the density of water at a certain temperature.

The **specific weight** of a fluid, designated by the Greek symbol  $\gamma$  (gamma), is defined as its *weight* per unit volume. Thus, specific weight is related to density through the equation

$$\gamma = \rho g \quad (1.6)$$

where  $g$  is the local acceleration of gravity. Just as density is used to characterize the mass of a fluid system, the specific weight is used to characterize the weight of the system. In the BG system,  $\gamma$  has units of  $\text{lb}/\text{ft}^3$  and in SI the units are  $\text{N}/\text{m}^3$ . Under conditions of standard gravity ( $g = 32.174 \text{ ft}/\text{s}^2 = 9.807 \text{ m}/\text{s}^2$ ), water at  $60^\circ\text{F}$  has a specific weight of  $62.4 \text{ lb}/\text{ft}^3$  and  $9.80 \text{ kN}/\text{m}^3$ . Tables 1.5 and 1.6 list values of specific weight for several common liquids (based on standard gravity). More complete tables for water can be found in Appendix B (Tables B.1 and B.2).

## 1.4.3 Specific Gravity

The **specific gravity** of a fluid, designated as  $SG$ , is defined as the ratio of the density of the fluid to the density of water at some specified temperature. Usually the specified temperature is taken as  $4^\circ\text{C}$  ( $39.2^\circ\text{F}$ ), and at this temperature the density of water is  $1.94 \text{ slugs}/\text{ft}^3$  or  $1000 \text{ kg}/\text{m}^3$ . In equation form, specific gravity is expressed as

$$SG = \frac{\rho}{\rho_{\text{H}_2\text{O}@4^\circ\text{C}}} \quad (1.7)$$

and since it is the *ratio* of densities, the value of  $SG$  does not depend on the system of units used. For example, the specific gravity of mercury at  $20^\circ\text{C}$  is 13.55. This is illustrated by the figure in the margin. Thus, the density of mercury can be readily calculated in either BG or SI units through the use of Eq. 1.7 as

$$\rho_{\text{Hg}} = (13.55)(1.94 \text{ slugs}/\text{ft}^3) = 26.3 \text{ slugs}/\text{ft}^3$$

or

$$\rho_{\text{Hg}} = (13.55)(1000 \text{ kg}/\text{m}^3) = 13.6 \times 10^3 \text{ kg}/\text{m}^3$$

It is clear that density, specific weight, and specific gravity are all interrelated, and from a knowledge of any one of the three the others can be calculated.

